Package 'Deriv'

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Type Package

Title Symbolic Differentiation

Version 4.3.6

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Description R-based solution for symbolic differentiation. It admits user-defined function as well as function substitution in arguments of functions to be differentiated. Some symbolic simplification is part of the work.

License GPL (>= 3)

Depends Rcpp, R (>= 4.5)

LinkingTo Rcpp

NeedsCompilation yes

Suggests testthat (>= 0.11.0)

BugReports https://github.com/sgsokol/Deriv/issues

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Imports methods

Encoding UTF-8

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`Deriv-package` *Symbolic Differentiation*

Description

R already contains two differentiation functions: D and deriv.

These functions have several limitations:

- the derivatives table can't be modified at runtime, and is only available in C.
- function cannot substitute function calls. eg:
  `f <- function(x, y) x + y; deriv(~f(x, x^2), "x")`

The advantages of this package include:

- It is entirely written in R, so would be easier to maintain.
- Can differentiate function calls:
  - if the function is in the derivative table, then the chain rule is applied.
  - if the function is not in the derivative table (or it is anonymous), then the function body is substituted in.
  - these two methods can be mixed. An entry in the derivative table need not be self-contained – you don't need to provide an infinite chain of derivatives.
- It's easy to add custom entries to the derivatives table, e.g.
  `drule[["cos"]] <- alist(x=-sin(x))`
- The output can be an executable function, which makes it suitable for use in optimization problems.
- Starting from v4.0, some matrix calculus operations are possible (contribution of Andreas Rappold). See an example in `help("Deriv")` for differentiation of the inverse of 2x2 matrix and whose elements depend on variable of differentiation `x`.

Details

Package:	Deriv
Type:	Package
Version:	4.2
Date:	2025-07-23
License:	GPL (>= 3)

Two main functions are Deriv() for differentiating and Simplify() for simplifying symbolically.

Author(s)

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References

https://andrewclausen.net/computing/deriv.html

See Also

D, deriv, packages Ryacas, rSymPy

Examples

```
## Not run: f <- function(x) x^2
## Not run: Deriv(f)
# function (x)
# 2 * x
```

`Deriv` *Symbolic differentiation of an expression or function*

Description

Symbolic differentiation of an expression or function

Usage

```
Deriv(
  f,
 x = if (is.function(f)) NULL else all.vars(if (is.character(f)) parse(text = f) else f),
  env = if (is.function(f)) environment(f) else parent.frame(),
  use.D = FALSE,
  cache.exp = TRUE,
  nderiv = NULL,
  combine = "c",
  drule = Deriv::drule
)
```

Arguments

`f` An expression or function to be differentiated. f can be

- a user defined function: `function(x) x**n`
- a string: `"x**n"`
- an expression: `expression(x**n)`
- a call: `call("^", quote(x), quote(n))`

- a language: `quote(x**n)`
- a right hand side of a formula: `~ x**n` or `y ~ x**n`

`x` An optional character vector with variable name(s) with respect to which `f` must be differentiated. If not provided (i.e. x=NULL), `x` is guessed either from `names(formals(f))` (if `f` is a function) or from all variables in f in other cases. To differentiate expressions including components of lists or vectors, i.e. by expressions like `p[1]`, `theta[["alpha"]]` or `theta$beta`, the vector of variables `x` must be a named vector. For the cited examples, the argument `x` must be given as follows `c(p="1", theta="alpha", theta="beta")`. Note the repeated name `theta` which must be provided for every component of the list `theta` by which a differentiation is required.

`env` An environment where the symbols and functions are searched for. Defaults to `parent.frame()` for `f` expression and to `environment(f)` if `f` is a function. For primitive function, it is set by default to .GlobalEnv

`use.D` An optional logical (default FALSE), indicates if base::D() must be used for differentiation of basic expressions.

`cache.exp` An optional logical (default TRUE), indicates if final expression must be optimized with cached sub-expressions. If enabled, repeated calculations are made only once and their results stored in cache variables which are then reused.

`nderiv` An optional integer vector of derivative orders to calculate. Default NULL value correspond to one differentiation. If length(nderiv)>1, the resulting expression is a list where each component corresponds to derivative order given in nderiv. Value 0 corresponds to the original function or expression non differentiated. All values must be non negative. If the entries in nderiv are named, their names are used as names in the returned list. Otherwise the value of nderiv component is used as a name in the resulting list.

`combine` An optional character scalar, it names a function to combine partial derivatives. Default value is "c" but other functions can be used, e.g. "cbind" (cf. Details, NB3), "list" or user defined ones. It must accept any number of arguments or at least the same number of arguments as there are items in `x`.

`drule` An optional environment-like containing derivative rules (cf. Details for syntax rules).

Details

R already contains two differentiation functions: `stats::D` and `stats:deriv`. `D` does simple univariate differentiation while `deriv` uses `D` to do multivariate differentiation. The output of `D` is an expression, whereas the output of `deriv` can be an executable function.

R's existing functions have several limitations. They can probably be fixed, but since they are written in C, this would probably require a lot of work. Limitations include:

- The derivatives table can't be modified at runtime, and is only available in C.
- Function cannot substitute function calls. e.g.: f <- function(x, y) x + y; deriv(~f(x, x^2), "x") is not working.

So, here are the advantages of this implementation:

- It is entirely written in R, so would be easier to maintain.
- Can do multi-variate differentiation.
- Can differentiate function calls:
  - if the function is in the derivative table, then the chain rule is applied. For example, if you declared that the derivative of `sin` is `cos`, then it would figure out how to call `cos` correctly in case of complex argument.
  - if the function is not in the derivative table (or it is anonymous), then the function body is substituted in.
  - these two methods can be mixed. An entry in the derivative table need not be self-contained – you don't need to provide an infinite chain of derivatives.
- It's easy to add custom entries to the derivatives table, e.g.

  `drule[["cos"]] <- alist(x=-sin(x))`

  The chain rule will be automatically applied if needed. In their custom rules, users should avoid using variable names like `.e1`, `.e2` etc. which can be confounded with those automatically created by `Deriv` for code caching purposes.
- The output is an executable function, which makes it suitable for use in optimization problems.
- Compound functions (i.e. piece-wise functions based on if-else operator) can be differentiated (cf. examples section).
- in case of multiple derivatives (e.g. gradient and hessian calculation), caching can make calculation economies for both
- Starting from v4.0, some matrix calculus operations are possible (contribution of Andreas Rappold). See an example hereafter for differentiation of the inverse of 2x2 matrix and whose elements depend on variable of differentiation `x`.

Two environments `drule` and `simplifications` are exported in the package's NAMESPACE. As their names indicate, they contain tables of derivative and simplification rules. To see the list of defined rules do `ls(drule)`. To add your own derivative rule for a function called say `sinpi(x)` calculating sin(pi*x), do `drule[["sinpi"]] <- alist(x=pi*cospi(x))`. Here, "x" stands for the first and unique argument in `sinpi()` definition. For a function that might have more than one argument, e.g. `log(x, base=exp(1))`, the drule entry must be a list with a named rule per argument. See `drule$log` for an example to follow. After adding `sinpi` you can differentiate expressions like `Deriv(~ sinpi(x^2), "x")`. The chain rule will automatically apply.

Starting from v4.0, user can benefit from a syntax `.d_X` in the rule writing. Here `X` must be replaced by an argument name (cf. `drule[["solve"]]` for an example). A use of this syntax leads to a replacement of this place-holder by a derivative of the function (chain rule is automatically integrated) by the named argument.
Another v4.0 novelty in rule's syntax is a possible use of optional parameter `` `_missing` `` which can be set to TRUE or FALSE (default) to indicate how to treat missing arguments. By default, i.e. in absence of this parameter or set to FALSE, missing arguments were replaced by their default values. Now, if `` `_missing`=TRUE `` is specified in a rule, the missing arguments will be left missed in the derivative. Look `drule[["solve"]]` for an example.

NB. In `abs()` and `sign()` function, singularity treatment at point 0 is left to user's care. For example, if you need NA at singular points, you can define the following: `drule[["abs"]] <- alist(x=ifelse(x==0, NA, sign(x)))` `drule[["sign"]] <- alist(x=ifelse(x==0, NA, 0))`

NB2. In Bessel functions, derivatives are calculated only by the first argument, not by the nu argument which is supposed to be constant.

NB3. There is a side effect with vector length. E.g. in `Deriv(~a+b*x, c("a", "b"))` the result is `c(a = 1, b = x)`. To avoid the difference in lengths of a and b components (when x is a vector), one can use an optional parameter `combine` `Deriv(~a+b*x, c("a", "b"), combine="cbind")` which gives `cbind(a = 1, b = x)` producing a two column matrix which is probably the desired result here. Another example illustrating a side effect is a plain linear regression case and its Hessian: `Deriv(~sum((a+b*x - y)**2), c("a", "b"), n=c(hessian=2)` producing just a constant `2` for double differentiation by `a` instead of expected result `2*length(x)`. It comes from a simplification of an expression `sum(2)` where the constant is not repeated as many times as length(x) would require it. Here, using the same trick with `combine="cbind"` would not help as all 4 derivatives are just scalars. Instead, one should modify the previous call to explicitly use a constant vector of appropriate length: `Deriv(~sum((rep(a, length(x))+b*x - y)**2), c("a", "b"), n=2)`

NB4. Differentiation of `*apply()` family (available starting from v4.1) is done only on the body of the `FUN` argument. It implies that this body must use the same variable names as in argument `x` and they must not appear in `FUN`s arguments (cf. GMM example).

NB5. Expressions are differentiated as scalar ones. However in some cases, obtained result remains valid if the variable of differentiation is a vector. This is just a coincidence. If you need to differentiate by vectors, you can try to write your own differentiation rule. For example, derivative of `sum(x)` where `x` is a vector can be done as: `vsum=function(x) sum(x) drule[["vsum"]] <- alist(x=rep_len(1, length(x)))` # drule is exported from Deriv namespace `Deriv(~vsum(a*x), "x", drule=drule)` # `a * rep_len(1, length(a * x))`

NB6. Since v4.2, it is possible to differentiate by named components of lists and vectors that are used in `with(data, expr)` expressions (cf. "with()" example). The names of argument `x` ("theta" in an example above) must be used directly, e.g `with(theta, ...)` or `with(as.list(theta), ...)`. Otherwise, the `expr` of `with()` will be differentiated as plain code.

Value

- a function if `f` is a function
- an expression if `f` is an expression
- a character string if `f` is a character string
- a language (usually a so called 'call' but may be also a symbol or just a numeric) for other types of `f`

Author(s)

Andrew Clausen (original version) and Serguei Sokol (actual version and maintainer)

See Also

Deriv_cpp

Examples

```
## Not run: f <- function(x) x^2
## Not run: Deriv(f)
```

```
# function (x)
# 2 * x

## Not run: f <- function(x, y) sin(x) * cos(y)
## Not run: Deriv(f)
# function (x, y)
# c(x = cos(x) * cos(y), y = -(sin(x) * sin(y)))

## Not run: f_ <- Deriv(f)
## Not run: f_(3, 4)
#              x         y
# [1,] 0.6471023 0.1068000

## Not run: Deriv(~ f(x, y^2), "y")
# -(2 * (y * sin(x) * sin(y^2)))

## Not run: Deriv(quote(f(x, y^2)), c("x", "y"), cache.exp=FALSE)
# c(x = cos(x) * cos(y^2), y = -(2 * (y * sin(x) * sin(y^2))))

## Not run: Deriv(expression(sin(x^2) * y), "x")
# expression(2*(x*y*cos(x^2)))

Deriv("sin(x^2) * y", "x") # differentiate only by x
"2 * (x * y * cos(x^2))"

Deriv("sin(x^2) * y", cache.exp=FALSE) # differentiate by all variables (here by x and y)
"c(x = 2 * (x * y * cos(x^2)), y = sin(x^2))"

# Compound function example (here abs(x) smoothed near 0)
fc <- function(x, h=0.1) if (abs(x) < h) 0.5*h*(x/h)**2 else abs(x)-0.5*h
Deriv("fc(x)", "x", cache.exp=FALSE)
"if (abs(x) < h) x/h else sign(x)"

# Example of a first argument that cannot be evaluated in the current environment:
## Not run:
  suppressWarnings(rm("xx", "yy"))
  Deriv(xx^2+yy^2)

## End(Not run)
# c(xx = 2 * xx, yy = 2 * yy)

# Automatic differentiation (AD), note intermediate variable 'd' assignment
## Not run: Deriv(~{d <- ((x-m)/s)^2; exp(-0.5*d)}, "x", cache.exp=FALSE)
#{
#   d <- ((x - m)/s)^2
#   .d_x <- 2 * ((x - m)/s^2)
#   -(0.5 * (.d_x * exp(-(0.5 * d))))
#}

# Custom differentiation rule
## Not run:
  myfun <- function(x, y=TRUE) NULL # do something useful
  dmyfun <- function(x, y=TRUE) NULL # myfun derivative by x.
```

```
  drule[["myfun"]] <- alist(x=dmyfun(x, y), y=NULL) # y is just a logical => no derivate
  Deriv(~myfun(z^2, FALSE), "z", drule=drule)
  # 2 * (z * dmyfun(z^2, FALSE))

## End(Not run)

# Differentiation by list components
## Not run:
  theta <- list(m=0.1, sd=2.)
  x <- names(theta)
  names(x)=rep("theta", length(theta))
  Deriv(~exp(-(x-theta$m)**2/(2*theta$sd)), x, cache.exp=FALSE)
# c(theta_m = exp(-((x - theta$m)^2/(2 * theta$sd))) *
#  (x - theta$m)/theta$sd, theta_sd = 2 * (exp(-((x - theta$m)^2/
#  (2 * theta$sd))) * (x - theta$m)^2/(2 * theta$sd)^2))

## End(Not run)

# Differentiation by list components used in "with()" expression (since v4.2)
# Compare with precedent example.
## Not run:
  theta <- list(m=0.1, sd=2.)
  x <- names(theta)
  names(x)=rep("theta", length(theta))
  Deriv(~with(theta, exp(-(x-m)**2/(2*sd))), x, cache.exp=FALSE)
# c(theta_m = with(theta, exp(-((x - m)^2/(2 * sd))) * (x - m)/sd),
#     theta_sd = with(theta, 2 * (exp(-((x - m)^2/(2 * sd))) *
#         (x - m)^2/(2 * sd)^2)))

## End(Not run)
# Differentiation in matrix calculus
## Not run:
 Deriv(~solve(matrix(c(1, x, x**2, x**3), nrow=2, ncol=2)))

## End(Not run)

# Two component Gaussian mixture model (GMM) example
## Not run:
# define GMM probability density function -> p(x, ...)
ncomp=2
a=runif(ncomp)
a=a/sum(a) # amplitude or weight of each component
m=rnorm(ncomp) # mean
s=runif(ncomp) # sd
# two column matrix of probabilities: one row per x value, one column per component
pn=function(x, a, m, s, log=FALSE) {
  n=length(a)
  structure(vapply(seq(n), function(i) a[i]*dnorm(x, m[i], s[i], log),
    double(length(x))), dim=c(length(x), n))
}
p=function(x, a, m, s) rowSums(pn(x, a, m, s)) # overall probability
dp=Deriv(p, "x")
# plot density and its derivative
```

```
xp=seq(min(m-2*s), max(m+2*s), length.out=200)
matplot(xp, cbind(p(xp, a, m, s), dp(xp, a, m, s)),
   xlab="x", ylab="p, dp/dx", type="l", main="Two component GMM")

## End(Not run)
```

`Deriv_cpp` *Symbolic Differentiation (Supports Vectors of Variables)*

Description

Computes the symbolic derivative of an R expression with respect to one or more target variables. If a single target is provided, it returns a scalar expression. If multiple targets are provided, it returns a named c() call.

Usage

```
Deriv_cpp(expr, x, env = parent.frame(), drule = Deriv::drule)
```

Arguments

`expr`	An R language object, symbol, or numeric constant to differentiate.
`x`	A character vector, symbol, or named vector of targets.
`env`	An environment to resolve function calls in (defaults to parent.frame()).
`drule`	An environment containing derivative rules (cf. Details in `Deriv` for syntax rules).

Details

This version is much faster for simple expressions but has less features than its R counterpart Deriv().

Value

A simplified R expression (or a named c() call for multiple inputs).

See Also

`Deriv`

format1 *Wrapper for base::format() function*

Description

Wrapper for base::format() function

Usage

```
format1(expr)
```

Arguments

expr	An expression or symbol or language to be converted to a string.

Value

A character vector of length 1 contrary to base::format() which can split its output over several lines.

Simplify *Symbollic simplification of an expression or function*

Description

Symbollic simplification of an expression or function

Usage

```
Simplify(expr, env = parent.frame(), scache = new.env())

Cache(st, env = Leaves(st), prefix = "")

deCache(st)
```

Arguments

expr	An expression to be simplified, expr can be • an expression: `expression(x+x)` • a string: `"x+x"` • a function: `function(x) x+x` • a right hand side of a formula: `~x+x` • a language: `quote(x+x)`
env	An environment in which a simplified function is created if `expr` is a function. This argument is ignored in all other cases.
scache	An environment where there is a list in which simplified expression are cached
st	A language expression to be cached
prefix	A string to start the names of the cache variables

Details

An environment `simplifications` containing simplification rules, is exported in the namespace accessible by the user. Cache() is used to remove redundunt calculations by storing them in cache variables. Default parameters to Cache() does not have to be provided by user. deCache() makes the inverse job – a series of assignements are replaced by only one big expression without assignement. Sometimes it is usefull to apply deChache() and only then pass its result to Cache().

Value

A simplified expression. The result is of the same type as `expr` except for formula, where a language is returned.

`Simplify_cpp` *Simplify Symbolic Expressions*

Description

Simplify Symbolic Expressions

Usage

```
Simplify_cpp(expr)
```

Arguments

`expr`	An R language object, symbol, or numeric constant to simplify.

Value

A simplified R expression or scalar numeric value.

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